# NEW MILFORD PUBLIC SCHOOLS 

New Milford, Connecticut


Honors Geometry
April 2023

## New Milford Board of Education

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## Authors of Course Guide

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## New Milford's Mission Statement

The mission of the New Milford Public Schools, a collaborative partnership of students, educators, family and community, is to prepare each and every student to compete and excel in an ever-changing world, embrace challenges with vigor, respect and appreciate the worth of every human being, and contribute to society by providing effective instruction and dynamic curriculum, offering a wide range of valuable experiences, and inspiring students to pursue their dreams and aspirations.

## Honors Geometry

9/10
This course is designed for students who have demonstrated high achievement in Honors Algebra 1. Geometry Topics in this course include geometric terminology, transformations, logical deductive proof, constructions, concept of congruence, similarity, parallelism, the study of polygons, circles, right triangles, volume and surface area and appropriate word problems. Algebraic concepts will be stressed. Calculators and/or computers will be used. A scientific calculator is required of all students in this course. At the honors level, this course is more rigorous by the inclusion of additional topics and more complex questions within each unit. This also includes a strong emphasis on review of algebraic topics, some incorporated into the geometric content and others that are reviewed in preparation for algebra 2 at the honors level.

## Vision of a Graduate

Honors Geometry lends itself to focus a great deal on creativity in drawing activities that are flexible and encourage students to create a unique product and on communication skills through proof writing and questions involving written explanations. In addition, students will learn to think critically and persevere in problem solving as they learn to identify key pieces of information, label diagrams and retrieve key facts or formulas in order to solve problems.

## Pacing Guide

| Unit 1 Transformations | $5-6$ weeks |
| :--- | ---: |
| Unit 2 Congruence, proof and construction | $5-6$ weeks |
| Unit 3 Properties of Triangles and Quadrilaterals | $5-6$ weeks |
| Midterm Exam - review and test | $1-2$ weeks |
| Unit 4 Similarity and Right Triangles | $7-8$ weeks |
| Unit 5 Volume and Surface Area | $5-6$ weeks |
| Unit 6 Properties of Circles | $5-6$ weeks |
| Final Exam - review and test | $1-2$ weeks |

## ESTABLISHED GOALS

## CCSS.MATH.CONTENT.HSG.CO.

 A. 1Know precise definitions of angle, circle, perpendicular line, parallel line, and line segment, based on the undefined notions of point, line, distance along a line, and distance around a circular arc.

## CCSS.MATH.CONTENT.HSG.CO.

 A. 2Represent transformations in the plane using, e.g., transparencies and geometry software; describe transformations as functions that take points in the plane as inputs and give other points as outputs. Compare transformations that preserve distance and angle to those that do not (e.g., translation versus horizontal stretch).

## CCSS.MATH.CONTENT.HSG.CO.

## A. 5

Given a geometric figure and a rotation, reflection, or translation, draw the transformed figure using, e.g., graph paper, tracing paper, or geometry software. Specify a sequence of transformations that

## Meaning

will carry a given figure onto another.

UNDERSTANDINGS
Students will understand that...

- Geometric terms and notation must be used correctly to ensure accurate communication of information.
- Functions can be used to change a figure's position and/or size.
- Functions can be used to represent a transformation in the coordinate plane.
- Figures are transformed by a composition of rigid motions and dilations, the corresponding angles of the image and preimage are congruent and the ratios of corresponding sides are proportional.
- Transformations can be created using a variety of tools, including technology,
- Dilations have a center and a radius
- Compositions of transformations can be used to make more complex patterns


## ESSENTIAL QUESTIONS

Students will keep considering...

- How does one express items in correct geometric terms?
- How can one change a figure's position without changing its size and shape?
- How can one change a figure's size without changing its shape?
- How can one represent a transformation in the coordinate plane?
- How can one recognize congruence and similarity in figures?
- How can transformations be used to create designs and tessellations?
- How can transformations describe a change in the position of an object?
- What are the properties of a figure preserved during a dilation?
- What does a composition of transformations look like?

Students will know..

- A transformation of a geometric figure is a change in its position, shape, or size.
- Some transformations preserve distance and angles while some do not.
- A transformation can be represented as a function
- A transformation can be created using a variety of mediums.
- A composition of transformations creates a more advanced pattern with additional properties

Students will be skilled at...

- Identifying and using Geometric vocabulary
- Observing patterns and developing definitions of reflections, rotations, and translations.
- Using geometric software and/or manipulatives to model and compare transformations.
- Demonstrating a sequence of transformations that will carry a figure onto another.
- Showing graphic representation of data
- Creating more advanced patterns using compositions of transformations and recognizing new properties within them.

STAGE 2

| Code | Evaluative Criteria | Assessment Evidence |
| :---: | :---: | :---: |
| T, M, A | Evaluative Criteria consists of <br> - an explanation of which transformations were used to design the pattern. <br> - accurate use of the transformation to create the pattern <br> - a final design that holds to the definition of a tessellation | PERFORMANCE TASK(S): <br> Goal: To design a character/animal based pattern for a child's bedding using tessellations <br> Role: Custom fabric/Interior designer <br> Audience: Owner of a store selling children's products <br> Situation: The manager of the store wants to introduce some new designs for the children's bedding that they sell. <br> Product: A completed tessellation design <br> Standards for Success: Scoring Rubric including focus on color, size and production of a tessellatable shape <br> Differentiation: Scaffolding where students can create a design from a simple transformation and basic coloring pattern or a more complex transformation and more sophisticated coloring scheme. |


|  | Evaluative criteria consists of: | OTHER EVIDENCE: |
| :---: | :---: | :---: |
| M, A | - Is the correct transformation created based on the vocabulary and/or function notation? | - Alternative assessment projects such as a logo design activity, graphing transformations on the coordinate plane, dilations with similar figures and designing patterns |
| M, A | - Is the correct vocabulary and/or notations used to represent a given transformation? | - Review of standardized test questions to prep students for the challenge of the SAT and ACT exams |
| T, M, A | - Are the appropriate transformations chosen for a specific application? | - Participation in class discussion, group work, and responses. |
| T, M, A | - Does the transformation model the desired application? | - Quizzes |
|  |  | - Unit Test - to include a variety of DOK level of problems and may include SAT style problems. |

- Teacher checks for prerequisite and prior knowledge via warm-up and questioning activities, such as basic problems on graphing vertical and horizontal lines and writing equations
- Prerequisite knowledge is reinforced through algebra review assignments
- Teacher will provide review and assessment on prerequisite geometric vocabulary knowledge to ensure all students are capable of communicating effectively

Summary of Key Learning Events and Instruction

- Teacher introduces vocabulary and notation associated with translations, reflections, rotations and dilations.

T, M, A

T, M, A

M, A

T, M, A

M, A

T, M, A

- Teacher demonstrates a variety of methods on how to complete an actual transformation using translations, reflections, rotations and dilations.
- Students use a variety of methods to complete transformations on worksheets, whiteboards and graph paper
- Students will observe patterns and develop definitions of reflections, rotations, translations and dilations
- Students will complete a project where they create an original shape and complete each of the 4 transformations on that shape
- Teacher expands upon their understanding of transformations through compound transformations and the results they achieve.
- Students practice working with compound transformations and sequences of transformations and identifying their results.

Progress Monitoring

- Monitoring class work through board work, group work, questioning, and walk-arounds
- Check for understanding via going over homework and mediums such as reflections and exit tickets
- Class worksheets with direct teacher observation or self assessment
- Practice on whiteboard/chalkboard with direct teacher observation
- Kahoot quiz or pear deck slideshow with review questions and direct teacher observation
- Reflective journals or exit tickets at the end of the lesson
- Edulastic or google form review assignments
- Homework assignments with direct teacher observation or self assessment

M, A

T, M, A

T, M, A

- Teacher introduces the concepts of symmetry and demonstrates them with physical models.
- Students will identify the symmetry associated with a variety of figures
- Students will create a shape that tessellates and use it to make a tessellation picture on paper.


## Suggested Resources and supplies

All Resources and materials must adhere to all New Milford Board of Education policies and regulations and are subject to New Milford Board of Education approval. Resources and materials must be researched and vetted by the writers and department heads prior to submission for approval.

- Textbook: Bass, Laurie, et.al. . Geometry Common Core. $1^{\text {st }}$ ed. Upper Saddle River, NJ: Pearson, Prentice Hall, 2012. Print.
- Textbook: Serra, Michael. Discovering Geometry. Emeryvillle, CA: Key Curriculum Press, 2008. Print.
- Resource materials provided by Pearson such as implementing the common core, differentiation and standardized test practice
- Resource from the Bureau of Education and Research: Strengthening your geometry program: Ideas, strategies and hands-on activities
- Geogebra; interactive application: Hohenwarter, Markus
- Kahoot; interactive game: Wiggins and Murphy
- Projects/performance tasks modeling real world problems involving all aspects of transformations and symmetry
- Summative assessments

> Quizzes
> Unit test

of rigid motions to decide if they are congruent.

- Angle relationships exist when parallel lines are intersected by a transversal.
- Geometric configurations can be constructed through the use of a variety of tools including technology
- Proof is the highest level of mathematical argument.
- Triangle congruence can be proven using geometric theorems
- Constructions of basic geometric shapes can be used to create more complex shapes.
- How can one find the measure of special angle pairs given parallel lines?
- How does one perform a geometric construction?
- How does one formulate a proof?


## Acquisition

Students will know...

- Algebraic properties can be used to introduce the concepts of proofs through work with algebraic equations
- Vocabulary: triangle, acute, obtuse, right, isosceles, scalene, equilateral, equiangular, interior angle, exterior angle,
- The criteria used to prove triangles congruent.(SAS, ASA, AAS, SSS and HL)
- That as a result of triangles being proven congruent, additional corresponding parts can identified as congruent(CPCTC)
- Vertical angles and the reflexive property play an important role in proving triangles congruent.
- The four special segments in triangles: median, altitude, angle bisector, perpendicular bisector..


## Students will be skilled at...

- Using algebraic properties to prove the solution to an algebraic equation is correct
- Identifying which theorem can be used to prove or disprove triangles congruent.
- Creating basic constructions for bisectors and congruent figures
- Proving and applying theorems about angles
- Using and applying the vertical angles theorem
- Identifying special angle pairs and relationships given two lines and a transversal
- Constructing basic geometric figures including but not limited to : congruent angles, bisectors, parallel and perpendicular lines
- Having a deeper understanding of the basic figures and how they can be used to create more advanced shapes such as

|  | - Constructions can be made to identify <br> a locus of points <br> Basic constructions can be combined <br> to create more advanced shapes and <br> to aid in the design of real world <br> diagrams and blueprints. | hexagons and trapezoids or in diagrams <br> of real world situations. |
| :--- | :--- | :--- |

STAGE 2

| Code | Evaluative Criteria | Assessment Evidence |
| :---: | :---: | :---: |
| T, M, A | Further information: | PERFORMANCE TASK(S): |
|  | Evaluative Criteria consists of: <br> - comprehensive explanation of corrections <br> - accurate use of mathematical concepts <br> - use of appropriate proof structure <br> - accurate completion of all tasks | Goal: To demonstrate how to communicate clearly using the medium of mathematical proof by correcting student mistakes |
|  |  | Role: Teacher |
|  |  | Audience: Student |
|  |  | Situation: Students will be given incorrect proofs. It will be their job to correct the mistakes and provide feedback. |
|  |  | Product: A completed worksheet with corrections clearly labeled with explanation. |
|  |  | Standards for Success: Rubric based on understanding of different styles of proof |
|  |  | Differentiation: Students will be able to choose from a variety of styles and difficulty level of proofs. |


|  | Evaluative criteria consists of: | OTHER EVIDENCE: |
| :---: | :---: | :---: |
| M, A | - Is there a clear understanding of vocabulary in terms of the connection to congruences when comparing geometric shapes? | - Alternative assessment projects such as a group proof activities, finding the mistake exercises or constructions involving real world criteria |
| M, A | - Is there a clear understanding of the format of a proof? | the challenge of the SAT and ACT exams |
| T, M, A | - Do the steps in the proof follow a logical order? | - Participation in class discussion, group work, and responses. |
| T, M, A | - Has a clear understanding of the purpose and outcome of the proof been communicated? | - Quizzes |
| M, A | - Are the correct steps followed in making a construction? | and may include SAT style problems. |
|  | - Does a construction accurately depict the desired outcome of a real-world application? |  |


| Code ${ }^{\text {M }}$ | Pre-Assessment <br> - Teacher checks for prerequisite and prior knowledge via warm-up and questioning activities, such as basic problems on geometric vocabulary as marked within a diagram <br> - Prerequisite knowledge is reinforced through algebra review assignments <br> - Teacher will provide review and assessment on prerequisite geometric vocabulary knowledge to ensure all students are capable of communicating effectively |  |
| :---: | :---: | :---: |
|  | Summary of Key Learning Events and Instruction | Progress Monitoring |
| M, A | - Teacher will introduce the methods of proof: statement/reason, flowchart and paragraph using prior knowledge on algebraic and geometric terms | - Monitoring class work through board work, group work, questioning, and walk-arounds |
| M, A | - Teacher will introduce the methods that do and do not prove triangles congruent. | - Check for understanding via going over homework and mediums such as reflections and exit tickets |
| T, M, A | - Students will complete proofs, using each method, to demonstrate their understanding of the logical sequence of steps and knowledge of vocabulary | - Class worksheets with direct teacher observation or self assessment |
| M, A | - Teacher reviews vocabulary and guides students in basic constructions of bisectors, perpendiculars, congruent figures. | - Practice on whiteboard/chalkboard with direct teacher observation <br> - Kahoot quiz or pear deck slideshow with |
| T, M, A | - Students will apply their knowledge of vocabulary and constructions to constructions of parallel lines, isosceles and equilateral triangles and rectangles. | review questions and direct teacher observation <br> - Reflective journals or exit tickets at the end of the lesson |
| T, M, A | - Students will use constructions to accurately depict solutions to real world situations and more complex shapes | - Edulastic or google form review assignments <br> - Homework assignments with direct teacher observation or self assessment |

## Suggested Resources and supplies

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- Projects/performance tasks modeling real world problems involving all aspects of proofs and constructions
- Summative assessments

Quizzes
Unit test

- Textbook: Bass, Laurie, et.al. . Geometry Common Core. $1^{\text {st }}$ ed. Upper Saddle River, NJ: Pearson, Prentice Hall, 2012. Print.
- Textbook: Serra, Michael. Discovering Geometry. Emeryvillle, CA: Key Curriculum Press, 2008. Print.
- Resource materials provided by Pearson such as implementing the common core, differentiation and standardized test practice
- Resource from the Bureau of Education and Research: Strengthening your geometry program: Ideas, strategies and hands-on activities
- Geogebra; interactive application: Hohenwarter, Markus
- Kahoot; interactive game: Wiggins and Murphy
- Geometer's Sketchpad; interactive application: KCP Technologies
- Desmos; advanced graphing calculator
- Google forms and Google slides with pear deck extension
- Supplies: Patty paper, compass, protractor, straight edge, graph paper, colored pencils,


## ESTABLISHED GOALS

CCSS.Math.Content.HSG.CO.C. 11
Prove theorems about parallelograms. Theorems include: opposite sides are congruent, opposite angles are congruent, the diagonals of a parallelogram bisect each other, and conversely, rectangles are parallelograms with congruent diagonals.

## CCSS.Math.Content.HSG.CO.

 C. 10Prove theorems about triangles. Theorems inc/ude: measures of interior angles of a triangle sum to $180^{\circ}$; base angles of isosceles triangles are congruent; the segment joining midpoints of two sides of a triangle is parallel to the third side and half the length; the medians of a triangle meet at a point.

CCSS.Math.Content.HSG.SRT. B. 4

Prove theorems about triangles. Theorems include: a

## Transfer

Students will be able to independently use their learning to...

- Work carefully to solve the problem and verify that calculations are accurate and solutions are reasonable.
- Solve problems by looking for and using rules, patterns, and experience with similar problems.
- Make sense of problems and persevere in solving them


## Meaning <br> UNDERSTANDINGS <br> ESSENTIAL QUESTIONS

- Special properties apply to isosceles and equilateral triangles
- Special segments in triangles exhibit specific properties in the real world.
- Two sides of a triangle must have a sum larger than the third.
- Properties of parallelograms work from specific (square) to general (parallelogram).
- Parallelograms use properties of parallel lines.
- Quadrilaterals can be determined through the slope and distance formula.
- Squares are rectangles, but a rectangle is not necessarily a square.
- Trapezoids and kites are special quadrilaterals which do not have the properties of parallelograms
- What distinguishes isosceles and equilateral triangles from other triangles?
- What are the special segments in triangles?
- What distinguishes the types of quadrilaterals?
- How does a square differ from a rectangle?
- How can we prove which quadrilateral we have?
- What are the properties of a trapezoid and kite, which separate it from a parallelogram?
- How are the interior and exterior angles in polygons calculated?
- How do the properties of the points of concurrency in a triangle relate to the real world?
line parallel to one side of a triangle divides the other two proportionally, and conversely; the Pythagorean Theorem proved using triangle similarity.

CCSS.Math. Content.HSG.SRT. B. 5

Use congruence and similarity criteria for triangles to solve problems and to prove relationships in geometric figures.

- Interior and exterior angles in polygons can be calculated using specific formulas
- Points of concurrency exist in all triangles as a result of the intersection of the special segments


## Acquisition

Students will know...

- Triangles can be broken into the more specific classifications: acute, obtuse, right, isosceles, scalene, equilateral, equiangular, and regular.
- The specific properties of each triangle
- The sum of interior angles in a triangle is 180 degrees.
- The four special segments in triangles: median, altitude, angle bisector, perpendicular bisector.
- Points of concurrency created by these special segments have real world applications
- The triangle inequality theorem states that the sum of any two sides must be longer than the third.
- The longest side in a triangle is across from the largest angle and the shortest side is across from the smallest angle.
- Quadrilaterals can be broken into the more specific classifications of: parallelograms, rectangles, rhombus, square, trapezoid and kite.
- The specific properties of each quadrilateral

Students will be skilled at...

- Identifying congruent angles and sides in an isosceles or equilateral triangle.
- Applying properties of special segments in triangles to problems using algebraic thinking.
- Calculating the length of a midsegment in a triangle.
- Finding the missing angle measures in a triangle.
- Using and applying Polygon Angle Sum Theorem.
- Using and applying Exterior Angle Theorem
- Proving the type of quadrilateral given information about the angles and sides.
- Showing the type of parallelogram by calculating slope and distance.
- Identifying the classification of parallelograms given the angle and side measurements.
- Giving a specific quadrilateral and coordinates (as variables) identify any missing coordinates (as variables).
- Applying properties of quadrilaterals to real-world problems.

|  | - The properties of midsegments in <br> triangles and trapezoids <br> -Polygons have interior and exterior <br> angles that can be calculated using <br> specific formulas | $\bullet$Calculating the interior and exterior <br> angles in polygons |
| :--- | :--- | :--- |

STAGE 2

Code Evaluative Criteria

|  |  | PERFORMANCE TASK(S): |
| :---: | :---: | :---: |
| T, M, A | Evaluative Criteria consists of: <br> - accurate use of mathematical concepts | Goal: To use knowledge of points of concurrency to physically locate a gift shop in an amusement park, a power line to a building and a circular train track connecting 3 sections of the amusement park |
|  | concurrency | Role: Architect |
|  | - correct method for construction of the point of concurrency | Audience: Owner of an amusement park |
|  | - complete explanation of final diagram and choice of location | Situation: The owner of an amusement park wants to move the gift shop to a location that is equidistant to the three main attractions at the park. He/she also wishes to construct a railroad connecting 3 outer sections of the park. He/she has hired the architect to help find this location. |
|  |  | Product: A diagram showing the location of the gift shop and railroad |
|  |  | Standards for Success: Rubric based on knowledge of points of concurrency and constructions. |
|  |  | Differentiation: Students will have the option to choose which of the construction tasks they would like to complete. |



## Pre-Assessment

- Teacher checks for prerequisite and prior knowledge via warm-up and questioning activities, such as basic problems on solving equations,order of operations and substitution
- Prerequisite knowledge is reinforced through algebra review assignments
- Teacher will provide review and assessment on prerequisite geometric vocabulary knowledge to ensure all students are capable of communicating effectively

Summary of Key Learning Events and Instruction

M, A

M, A

T, M, A

T, M, A

M, A

T, M, A

- Teacher will guide students through a review of prior knowledge on triangles including median, altitude, perpendicular bisector and angle bisector
- Teacher will introduce properties of triangles: sum of interior angles, exterior angle theorem, isosceles triangles, triangle inequality theorem, and longest/shortest side relationship to smallest/largest angle
- Student knowledge will be reinforced through a discovery lesson using linguini and measuring activities
- Students will apply knowledge of vocabulary and properties of triangles on class practice with direct monitoring from the teacher
- Teacher will introduce the vocabulary associated with points of concurrency
- Students will demonstrate their understanding of points of concurrency through a construction project requiring application of content to specific scenarios.

Progress Monitoring

- Monitoring class work through board work, group work, questioning, and walk-arounds
- Check for understanding via going over homework and mediums such as reflections and exit tickets
- Class worksheets with direct teacher observation or self assessment
- Practice on whiteboard/chalkboard with direct teacher observation
- Kahoot quiz or pear deck slideshow with review questions and direct teacher observation
- Reflective journals or exit tickets at the end of the lesson
- Edulastic or google form review assignments
- Homework assignments with direct teacher observation or self assessment

| M, A | - Teacher will guide students through a review of prior knowledge on quadrilaterals | - Projects/performance tasks modeling real world problems involving all aspects of the properties of triangles and quadrilaterals |
| :---: | :---: | :---: |
| M, A | - Teacher will introduce the family tree of quadrilaterals. | - Summative assessments |
| T, M, A | - Students will apply knowledge of properties of triangles and quadrilaterals to coordinate geometry proofs using midpoint, distance and slope to identify specific triangles and quadrilaterals | Quizzes <br> Unit test |
| T, M, A | - Students will apply knowledge of vocabulary and properties of quadrilaterals on class practice with direct monitoring from the teacher |  |
| T, M, A | - Students will demonstrate understanding of vocabulary and properties of triangles and quadrilaterals through construction activities involving equilateral and isosceles triangles, squares, rectangles, rhombus, parallelograms and hexagons. |  |
| M, A | - Students will use a discovery lesson to determine the polygon angle sum theorem |  |
| T, M, A | - Students will apply their knowledge of interior and exterior angles to application problems with direct monitoring from the teacher |  |
|  | Suggested Resources and supplies |  |
|  | All Resources and materials must adhere to all New Milford Board of Education policies and regulations and are subject to New Milford Board of Education approval. Resources and materials must be researched and vetted by the writers and department heads prior to submission for approval. |  |

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- Resource from the Bureau of Education and Research: Strengthening your geometry program: Ideas, strategies and hands-on activities
- Geogebra; interactive application: Hohenwarter, Markus
- Kahoot; interactive game: Wiggins and Murphy
- Geometer's Sketchpad; interactive application: KCP Technologies
- Desmos; advanced graphing calculator
- Google forms and Google slides with pear deck extension
- Supplies: Patty paper, compass, protractor, straight edge, graph paper, colored pencils, linguini

Subject/Course: Honors Geometry Grade:9/10
Time frame: approx $7-8$ weeks

## ESTABLISHED GOALS

CCSS.Math.Content.HSG.SRT.A .
Given two figures, use the definition of similarity in terms of similarity transformations to decide if they are similar; explain using similarity transformations the meaning of similarity for triangles as the equality of all corresponding pairs of angles and the proportionality of all corresponding pairs of sides. corresponding pairs of sides.
CCSS.Math.Content.HSG.SRT. C. 6

Understand that by similarity, side ratios in right triangles are properties of the angles in the triangle, leading to definitions of trigonometric ratios for acute angles.

CCSS.Math.Content.HSG.SRT. C. 8

## UNDERSTANDINGS

Students will understand that...

- Similarity refers to any objects which have the same shape.
- Ratio and proportion can be used often to find missing sides in similar figures.
- Sides and angles in a right triangle can be calculated using several different methods.
- Classification of a triangle as acute, right or obtuse can be found using the pythagorean theorem.
Students will be able to independently use their learning to... are reasonable. problems.
- Make sense of problems and persevere in solving them


## Transfer

- Work carefully to solve the problem and verify that calculations are accurate and solutions
- Solve problems by looking for and using rules, patterns, and experience with similar


## Meaning

## ESSENTIAL QUESTIONS

Students will keep considering...

- How can we show two triangles are similar?
- How can we identify corresponding parts of similar triangles?
- How can we find the length of the side in a right triangle without Pythagorean theorem?
- How can the Pythagorean theorem determine the classification of a triangle

Use trigonometric ratios and the Pythagorean Theorem to solve right triangles in applied problems.

## CCSS.Math.Content.HSG.GPE

 A. 1Derive the equation of a circle of given center and radius using the Pythagorean Theorem; complete the square to find the center and radius of a circle given by an equation.

CCSS.MATH.CONTENT.HSG. SRT.A. 3

Use the properties of similarity transformations to establish the AA criterion for two triangles to be similar

- Special right triangles have formulas to identify exact values for side lengths
- Unit circle coordinates are derived using the values of special triangles
- Ratios are used in all right triangles using the sine, cosine or tangent of an angle.
- Sine and cosine of complementary angles are congruent.
- Angles of elevation and depression are angles formed above and below a horizontal plane.
- Distance formula and equation of a circle are both derived from the pythagorean theorem
- How can we find the missing parts of a right triangle?
- How do special triangles relate to finding the coordinates in a unit circle?
- How can we use ratios to find missing parts of triangles?
- How do we apply the shortcuts for special right triangles?
- What is the Golden Ratio?
- How do trigonometric ratios relate to similar right triangles?
- What is the difference between an angle of elevation and an angle of depression?
- How to write the equation of a circle and use it to graph the circle?
- How to find the distance between two points?


## Acquisition

Students will know...

- Vocabulary: Right Triangle, Hypotenuse, Adjacent Leg, Opposite Leg.
- Ratios are used to find missing parts of similar figures.
- Similar figures are the same shape but not necessarily the same size.
- Similar figures may be congruent, but congruent figures are always similar.
- The shortcuts for similarity are AA, SAS, SSS
- 30-60-90 and 45-45-90 are the most common configurations of right triangles.
- Using the Pythagorean Theorem we can prove shortcuts to find exact

Students will be skilled at...

- Using trigonometry to find a missing side or missing angle in a right triangle.
- Using special right triangles, find the exact value of a side in a right triangle
- Applying similarity to find the length of real-world objects like the height of an outdoor flagpole.
- Proving similarity in triangles with the AA similarity criterion.
- Identifying three natural locations where the Golden Ratio appears.
- Applying the Pythagorean Theorem and its converse to triangles
- Using the rules for special triangles to find coordinates of the unit circle

|  | lengths of sides for special right triangles. <br> - The coordinates in unit circles can be found using the rules for special triangles <br> - Sine and Cosine of complementary angles are congruent. <br> - Trigonometric ratios can be used to find a missing length or angle measure in a triangle <br> - Distance formula and equation of a circle are both derived from the pythagorean theorem | - Applying the sine, cosine and tangent ratios to real-world application problems. <br> - Classifying and solving problems involving angles of elevation and depression <br> - Calculating distances using two coordinates <br> - Using the equation of a circle to graph the circle |
| :---: | :---: | :---: |


| Code | Evaluative Criteria | Assessment Evidence |
| :---: | :---: | :---: |
| M | Evaluative Criteria consists of: <br> - accurate use of mathematical concepts <br> - identification of one of the appropriate methods for the calculation <br> - precise measurements and calculations <br> - complete explanation of final result | PERFORMANCE TASK(S): <br> Goal: Calculate the height of the flagpole outside the high school <br> Role: Engineer <br> Audience: Board of Education <br> Situation: The Board of Education would like to purchase a new flagpole and would like to know the height of the current flagpole. <br> Product: Work shown with diagram and written summary about which size pole to purchase <br> Standards for Success: Rubric based on the method of calculation and accuracy of solution <br> Differentiation: Students will be able to choose which mathematical method they would like to use to complete the task. |



- Teacher checks for prerequisite and prior knowledge via warm-up and questioning activities, such as basic problems on cross multiplication, simplifying radicals and solving equations
- Prerequisite knowledge is reinforced through algebra review assignments
- Teacher will provide review and assessment on prerequisite geometric vocabulary knowledge to ensure all students are capable of communicating effectively

Summary of Key Learning Events and Instruction

M, A

- Teacher will guide students through a review of prior knowledge on Corresponding Angles, Corresponding Sides, Congruence Statements, and Scale Factor (Similarity Ratio)

M, A

T, M, A

M, A

T, M, A

T, M, A

- Teacher will introduce new vocabulary: Right Triangle, Hypotenuse, Adjacent Leg, Opposite Leg, Trigonometric Ratios, Angle of Elevation, Angle of Depression
- Students will demonstrate their understanding of the vocabulary on class practice with direct monitoring from the teacher
- Teacher will introduce triangle similarity using AA, SAS, and SSS similarity criterion.
- Teacher will guide students through a review of prior knowledge of the pythagorean theorem and its applications, and introduce its relation to the distance formula and the equation of a circle
- Teacher will derive the formulas for special triangles using the pythagorean theorem.

Progress Monitoring

- Monitoring class work through board work, group work, questioning, and walk-arounds
- Check for understanding via going over homework and mediums such as reflections and exit tickets
- Class worksheets with direct teacher observation or self assessment
- Practice on whiteboard/chalkboard with direct teacher observation
- Kahoot quiz or pear deck slideshow with review questions and direct teacher observation
- Reflective journals or exit tickets at the end of the lesson
- Edulastic or google form review assignments
- Homework assignments with direct teacher

T, M, A

M, A

T, M, A

T, M, A

- Students will apply knowledge of pythagorean theorem and special triangles to applications and problems involving the unit circle and equation of a circle.
- Teacher will introduce trigonometric ratios and SOHCAHTOA to find a missing side or missing angle in a right triangle.
- Students will apply knowledge of similarity, pythagorean theorem and trigonometry to real applications with direct monitoring from the teacher and peer and self assessment
- Students will apply their knowledge from this unit to choose an appropriate method to find the height of the flagpole in front of the school.


## Suggested Resources and supplies

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- Textbook: Bass, Laurie, et.al. . Geometry Common Core. $1^{\text {st }}$ ed. Upper Saddle River, NJ: Pearson, Prentice Hall, 2012. Print.
- Textbook: Serra, Michael. Discovering Geometry. Emeryvillle, CA: Key Curriculum Press, 2008. Print.
- Resource materials provided by Pearson such as implementing the common core, differentiation and standardized test practice
observation or self assessment
- Projects/performance tasks modeling real world problems involving all aspects of right triangles
- Summative assessments


## Quizzes

Unit test

|  | - Resource from the Bureau of Education and Research: Strengthening your geometry program: Ideas, strategies and hands-on activities <br> - Geogebra; interactive application: Hohenwarter, Markus <br> - Kahoot; interactive game: Wiggins and Murphy <br> - Geometer's Sketchpad; interactive application: KCP Technologies <br> - Desmos; advanced graphing calculator <br> - Google forms and Google slides with pear deck extension <br> - Supplies: white boards, straight edge, graph paper, colored pencils, clinometer, measuring tape |  |
| :---: | :---: | :---: |

Subject/Course: Honors Geometry Grade:9/10
Time frame: approx $5-6$ weeks

## ESTABLISHED GOALS

CCSS.Math.Content.HSG.GMD. A. 3

Use volume formulas for cylinders, pyramids, cones, and spheres to solve problems.

CCSS.Math.Content.HSG.GM D.B. 4

Identify the shapes of two-dimensional cross-sections of three-dimensional objects, and identify three-dimensional objects generated by rotations of two-dimensional objects.

CCSS.Math.Content.HSG.MG. A. 2

Apply concepts of density based on area and volume in modeling situations (e.g., persons per square mile, BTUs per cubic foot)."


- Bases of a prism can be found by identifying the non-rectangular parallel faces of the solid (with the exception of a rectangular prism).
- Base of a pyramid can be found by identifying the non triangular face of the solid (with the exception of a triangular pyramid)
- Slant height of a shape is different than the actual height
- Units which are reported in an answer are critical to the accuracy of an answer.
- Cross section is the intersection of a solid and a plane.
- Area and volume calculations are utilized in numerous career fields
- Density and displacement formulas are used as an extension for volume
- Similar solids have the same shape and all their corresponding dimensions are proportional. If the scale factor of two similar solids is $a: b$, then the ratio of their corresponding surface areas is $a^{2}: b^{2}$, and the ratio of their volumes is $a^{3}: b^{3}$.
- How is the cross section of a shape used in calculating surface area and volume?
- How are area and volume used in real life career fields?
- Why are units important to the accuracy of an answer?
- What is the purpose of the cross section of a solid?
- How does the slant height differ from the actual height of a solid?
- How do the surface areas and volumes of similar solids compare?
- What role does volume play in finding the density and displacement of an object?


## Acquisition

Students will know...
Students will be skilled at...

- The Formulas for area of two-dimensional figures.
- Vocabulary: Polyhedron, prism, pyramid, cylinder, cone, sphere, hemisphere, height, base, apothem,
- Applying the formulas for surface area and volume to prisms, pyramids, cylinders, and spheres.
- Relating cross sections to the calculations of surface area and volume.


| Code | Evaluative Criteria | Assessment Evidence |
| :---: | :---: | :---: |
| T, M, A | Evaluative Criteria consists of: <br> - Accurate use of mathematical concepts <br> - Identification of the appropriate formula for each shape <br> - Precise measurements and calculations <br> - Complete explanation of final results | PERFORMANCE TASK(S): <br> Goal: Find the surface area and volume of compound solids that are used for storage (i.e. silos, sheds and barns) <br> Role: Design employee at a construction company <br> Audience: Builders at the construction company <br> Situation:Builders need the specifications for building the silos, sheds and barns that the company sells. <br> Product: Work/Calculations and conclusion about the materials needed to produce each storage unit. <br> Standards for Success: Rubric based on accurate data collection and presentation of conclusions. <br> Differentiation: Students will work hands-on with 3-dimensional shapes that require the use of basic and familiar area and volume formulas as well as the option to work with shapes that require the use of more complex formulas and calculations. |


|  |  | OTHER EVIDENCE: |
| :---: | :---: | :---: |
|  | Evaluative criteria consists of: |  |
| T, M, A | - Is the correct calculation(i.e. area, surface area or volume) used to solve the problem? | - Alternative assessment projects such as labs involving measuring and calculating volumes and surface areas of real objects, questioning activities that identify which |
| M, A | - Is the correct solid and corresponding formula identified for use in solving the problem? | and applications involving real world volume and surface area calculations. |
| M, A | - Are all values been measured accurately | - Review of standardized test questions to prep students for the challenge of the SAT and ACT exams |
| M,A | - Is the solution the result of accurate substitution and calculation | - Participation in class discussion, group work, and responses. |
| M,A | - Is the solution labeled with the correct units | - Quizzes |
| T, M, A | - Are the answers to a real world problem clearly communicated? | - Unit Test - to include a variety of DOK level of problems and may include SAT style problems. |

## Pre-Assessment

- Teacher checks for prerequisite and prior knowledge via warm-up and questioning activities, such as basic problems on substitution, order of operations, solving equations and identification of basic shapes
- Prerequisite knowledge is reinforced through algebra review assignments
- Teacher will provide review and assessment on prerequisite geometric vocabulary knowledge to ensure all students are capable of communicating effectively

Summary of Key Learning Events and Instruction

T, M, A

- Teacher will guide students through a review of prior knowledge on area formulas
- Teacher will introduce and demonstrate the concepts of cross sections and solids of revolutions and relate them to the calculation of volume and surface area
- Teacher will guide students through a review of prior knowledge on surface area, both by formula and the sum of individual sides
- Teacher will guide the students through a demonstration of the volume of pyramids and cones as they relate to prisms and cylinders and will acknowledge the formulas for each shape
- Students will practice measuring skills by calculating the surface area and volume for a wide range of three-dimensional solids. This will be in a laboratory format.
- Teacher will brainstorm with students how to determine if a problem is asking for area, surface area and volume.

Progress Monitoring

- Monitoring class work through board work, group work, questioning, and walk-arounds
- Check for understanding via going over homework and mediums such as reflections and exit tickets
- Class worksheets with direct teacher observation or self assessment
- Practice on whiteboard/chalkboard with direct teacher observation
- Kahoot quiz or pear deck slideshow with review questions and direct teacher observation
- Reflective journals or exit tickets at the end of the lesson
- Edulastic or google form review assignments
- Homework assignments with direct teacher observation or self assessment
- Projects/performance tasks modeling real

T, M, A

T, M, A

T, M, A

T, M, A

T, M, A

M, A

T, M, A

- Teacher will have students work in groups to create and solve their own application problems for surface area and volume
- Students will apply area formulas to solve both single
- Students will explore various occupations that use these formulas and perform some of the calculations.
- Teacher will model how to determine an object's composition based on its density.
- Students will work individually to calculate density of an irregular shaped solid to determine its volume and composition.
- Teacher will introduce the concept of scale factors for areas and volumes through a group discovery activity and subsequent class analysis of the results
- Students will work in groups to "think, pair, and share" results about the relationship between scale factors, areas, and volumes of similar solids.


## Suggested Resources and supplies

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world problems involving all aspects of area, surface area and volume

- Summative assessments

Quizzes
Unit test

- Textbook: Bass, Laurie, et.al. . Geometry Common Core. $1^{\text {st }}$ ed. Upper Saddle River, NJ: Pearson, Prentice Hall, 2012. Print.
- Textbook: Serra, Michael. Discovering Geometry. Emeryville, CA: Key Curriculum Press, 2008. Print.
- Resource materials provided by Pearson such as implementing the common core, differentiation and standardized test practice
- Resource from the Bureau of Education and Research: Strengthening your geometry program: Ideas, strategies and hands-on activities
- Geogebra; interactive application: Hohenwarter, Markus
- Kahoot; interactive game: Wiggins and Murphy
- Geometer's Sketchpad; interactive application: KCP Technologies
- Desmos; advanced graphing calculator
- Google forms and Google slides with pear deck extension
- Supplies: white boards, rulers, colored pencils, 2-d and 3-d shapes, manipulatives for cross sections and solids of rotation.

Subject/Course: Honors Geometry Grade:9/10
Time frame: approx 5-6 weeks

Unit: 6 Circles

## ESTABLISHED GOALS

CCSS.Math.Content.HSG.C.A. 2 Identify and describe relationships among inscribed angles, radii, and chords. Include the relationship between central, inscribed, and circumscribed angles; inscribed angles on a diameter are right angles; the radius of a circle is perpendicular to the tangent where the radius intersects the circle.
CCSS.MATH.CONTENT.HSG.C. A. 1

Prove that all circles are similar

## CCSS.MATH.CONTENT.HSG.

 C.A. 3Construct the inscribed and circumscribed circles of a triangle, and prove properties of angles for a quadrilateral inscribed in a circle.

## Transfer

Students will be able to independently use their learning to...

- Work carefully to solve the problem and verify that calculations are accurate and solutions are reasonable.
- Solve problems by looking for and using rules, patterns, and experience with similar problems.
- Make sense of problems and persevere in solving them


## UNDERSTANDINGS

Students will understand that...

- A circle is the set of all points equidistant from the center.
- Arcs and angles are closely related but the notation is different.
- Area of a sector is a fractional piece of the area of the entire circle.
- Central angles and inscribed angles will have different sized arcs.
- Arc length is a fractional piece of the circumference.
- Properties of tangents, secants and chords can be used to determine segment lengths in circles
- Tangents and radii meet at right angles
- Chords that are bisected by a diameter are also perpendicular
- Right triangles can be formed within circles using the properties of circles and then used to solve for missing measurements
- Right triangles within circles create areas that can be calculated and provide real world application.


## ESSENTIAL QUESTIONS

Students will keep considering...

- What are the key terms for a circle?
- How are arc measure and angle measure related?
- How does one measure arc length and how is it related to the circumference of a circle?
- How can segment lengths be calculated using properties of tangents, secants and chords?
- How can the right angle formed by a tangent and radius can be used to identify right triangles within a diagram?
- How does a diameter that is a perpendicular bisector of a chord create a right triangle within a diagram?
- How can triangles within circles create areas that have real applications?


## Acquisition

Students will know...

- Vocabulary: Circle, Radius, Diameter, Chord, Arc, Sector, Angle, Intercepted Arc, Inscribed Angle, Central Angle, tangent, secant.
- Inscribed Angle measures are half the measure of the arc.

Students will be skilled at...

- Calculating measure of an arc.
- Calculating measure of an interior angle.
- Calculating measure of an inscribed angle.
- Calculating the arc length.
- Calculating the area of a sector.


| Code | Evaluative Criteria | Assessment Evidence |
| :---: | :---: | :---: |
| T, M, A | Evaluative Criteria consists of: <br> - accurate use of mathematical concepts <br> - identification of the appropriate term and formula for each computation <br> - precise measurements and calculations <br> - complete explanation of final results | PERFORMANCE TASK(S): <br> Goal: To calculate the measures of lines, sectors and angles on a standard oval track. <br> Role: Surveyor <br> Audience: Manager of a development company <br> Situation: Use the properties of circles, tangents and chords to calculate the distances and angle measures of a standard oval track. <br> Product: Calculated distances and angle measures for each proposed situation. <br> Standards for Success: Rubric based on accurate data collection and presentation of conclusions. <br> Differentiation: Students will be able to choose from a variety of different methods to solve the problems. |


|  |  | OTHER EVIDENCE: |
| :---: | :---: | :---: |
|  | Evaluative criteria consists of: |  |
| $T, M, A$$M, A$ | - Is all given information correctly labeled in the diagram? | - Alternative assessment projects such as real world |
|  | - Is the correct vocabulary term and corresponding formula identified in solving the problem? | applications involving the properties of circles, more complex problems involving properties of triangles within circles and problems incorporating areas of shaded regions in more complex diagrams. |
| T, M, A | - Are the properties of the segments identified and used to determine the existence of right triangles within the diagram? | - Review of standardized test questions to prep students for the challenge of the SAT and ACT exams <br> - Participation in class discussion, group work, and responses. |
| M, A | - Are calculations and solutions completed accurately? | - Quizzes |
|  |  | - Unit Test - to include a variety of DOK level of problems and may include SAT style problems. |

stage 3

## Pre-Assessment

- Teacher checks for prerequisite and prior knowledge via warm-up and questioning activities, such as basic problems on substitution, solving equations, order of operations and identification of basic parts of a circle
- Prerequisite knowledge is reinforced through algebra review assignments
- Teacher will provide review and assessment on prerequisite geometric vocabulary knowledge to ensure all students are capable of communicating effectively

Summary of Key Learning Events and Instruction

- Teacher will guide students in the definition of key terms.
- Teacher will confirm with students the measure of
angles using a protractor.
- Students will explore the measure of arc and angles using an activity to measure angles.
- Teacher will describe how tangents, secants and line segments are related to circles
- Students will demonstrate their understanding of tangents, secants, angles and arcs through class practice on whiteboards and worksheets
- Teacher will describe the various situations where segments are divided on tangents and secants and the corresponding formulas used to determine their lengths
- Teacher will demonstrate how properties of segments can lead to the formation of a right triangle within the diagram that can be used to solve the problem

Progress Monitoring

- Monitoring class work through board work, group work, questioning, and walk-arounds
- Check for understanding via going over homework and mediums such as reflections and exit tickets
- Class worksheets with direct teacher observation or self assessment
- Practice on whiteboard/chalkboard with direct teacher observation
- Kahoot quiz or pear deck slideshow with review questions and direct teacher observation
- Reflective journals or exit tickets at the end of the lesson
- Edulastic or google form review assignments
- Homework assignments with direct teacher observation or self assessment

T, M, A

T, M, A

T, M, A

- Students will complete a variety of real world problems involving circles and right triangles.
- Students will complete a hands-on activity to measure the lines, sectors and angles involved in Track \& Field.
- Students will identify the relationship between central, inscribed interior and exterior angles and apply them to real applications


## Suggested Resources and supplies

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- Geogebra; interactive application: Hohenwarter, Markus
- Kahoot; interactive game: Wiggins and Murphy
- Geometer's Sketchpad; interactive application: KCP Technologies
- Desmos; advanced graphing calculator
- Projects/performance tasks modeling real world problems involving all aspects of the properties of circles
- Summative assessments

Quizzes
Unit test

| $\bullet$ | Google forms and Google slides with pear deck <br> extension |  |
| :--- | :--- | :--- |
| Supplies: white boards, graph paper, colored pencils, <br> 2-d and 3-d shapes, compass |  |  |

