

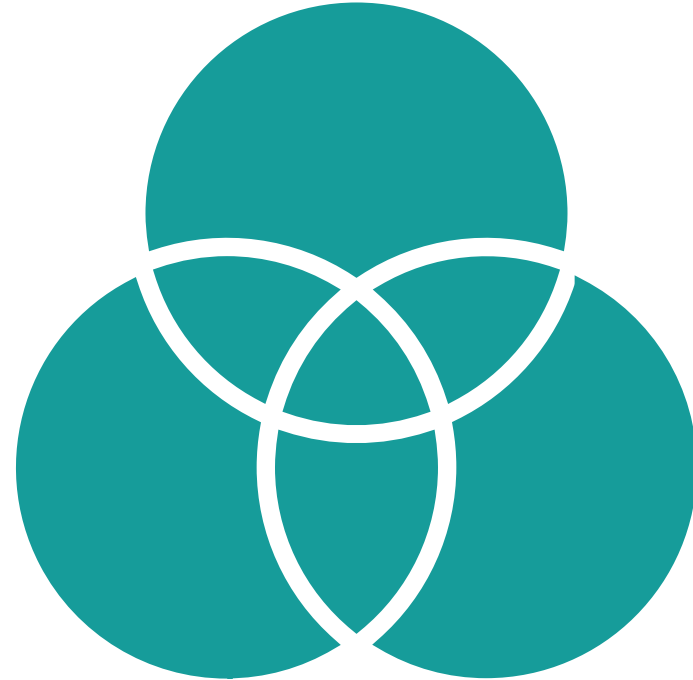
PROPORTIONAL TABLE

7th Grade - Math

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Objectives

- Comprehend that the phrase “proportional relationship” refers to when two quantities are related by multiplying by a “constant of proportionality.”
- Describe relationships between rows or between columns in a table that represents a proportional relationship.
- Explain how to calculate missing values in a table that represents a proportional relationship.

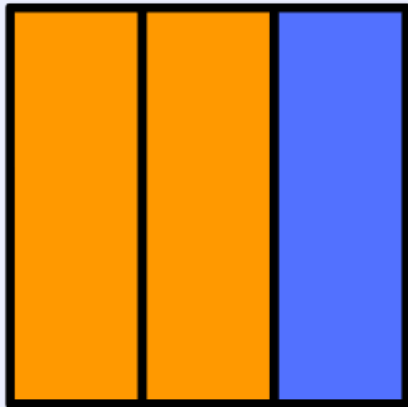


Ratio

- A ratio compares two quantities, and a proportion indicates that the relationship between those quantities is the same in both ratios.

A **ratio** is a relation that compares two numbers or quantities.

You can compare two parts to each other or to the whole.

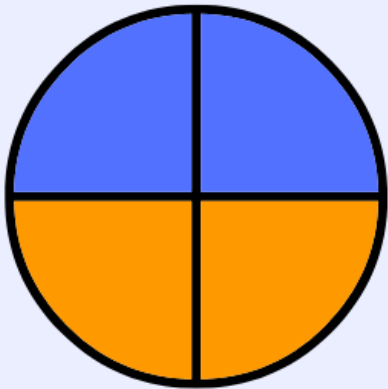


2:1	1:2	2:3	1:3
2/1	1/2	2/3	1/3
2 to 1	1 to 2	2 to 3	1 to 3

Proportion

- A proportion is an equation that states two ratios are equal.

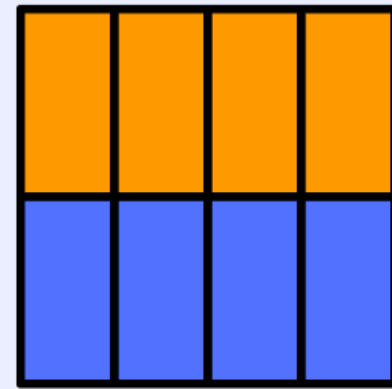
A **proportion** is a statement or equation that equates two ratios.



$$2:2 = 4:4$$

$$2:2 :: 4:4$$

2 is to 2 as 4 is to 4



Key Concept

- **Ratio:** A comparison of two quantities, often written as a fraction or with a colon (e.g., 2:5 or $2/5$).
- **Proportion:** An equation that shows two ratios are equal, like $2/5 = 4/10$.
- **Terms of a proportion:** In a proportion $a : b :: c : d$ (or $a/b = c/d$), the terms are a, b, c, and d.
- **Extremes:** The first and last terms in a proportion (a and d).
- **Means:** The middle two terms in a proportion (b and c).

How to Check for a Proportion

- You can determine if two ratios form a proportion by checking if the cross-products are equal.
 - *For the proportion $a : b :: c : d$, the cross-product is found by multiplying the means ($b \times c$) and the extremes ($a \times d$). If $a \times d = b \times c$, then the proportion is true.*

Proportional Relationship

- A **proportional relationship** is a connection between two variables where their ratio remains constant, meaning one variable is always a multiple of the other by the same factor, known as the constant of proportionality (k).

PACMAN RACE

Pacman traveled 18 feet every 6 seconds.

Pacman's distance traveled is proportional to time.

Constant of Proportionality

$$k = \underline{\hspace{2cm}}$$

Time (seconds)	Distance (feet)
0	
1	
2	
3	
4	
5	
6	18

Are these tables proportional?

x	y
3	12
5	20
8	32
10	40

Time (hours)	Snowfall (inches)
2	8
2.5	10
4	12
6	18

x	0	2	4
y	0	5	10

These tables are proportional. Find k and the missing values.

x	y
3	12
6	24
9	
	40

Gas (gallons)	Distance (miles)
2	36
2.5	
5	90
6	108

Use the verbal statement to fill in the table. Find the constant of proportionality, k .

1. Teri pays 4 dollars for 2 gallons of milk.

Milk (gallons)	Cost (dollars)
0	
1	
2	
3	
4	

$$k = \underline{\hspace{2cm}}$$

2. Patrick eats 15 crabby patties every 3 hours.

Time (hours)	Patties (#)
0	
1	
2	
3	
4	

$$k = \underline{\hspace{2cm}}$$

In each table, determine if y is proportional to x . Explain why or why not.

3.

x	y
3	12
5	20
8	32
10	40

Proportional? YES or NO

Explanation:

4.

x	y
4	2
6	3
10	5

Proportional? YES or NO

Explanation:

5.

x	y
1	4
4	8
6	24
9	18

Proportional? YES or NO

Explanation:

6.

x	12	18	15	9
y	4	6	5	3

Proportional? YES or NO

Explanation:

7.

x	0	2	4
y	0	5	10

Proportional? YES or NO

Explanation:

8.

x	0	1	2	3
y	3	5	7	9

Proportional? YES or NO

Explanation:

Use the tables to answer the following.

9.

Candy (pounds)	Cost (dollars)
6	12
3	5
7	14
2	4

Is the cost proportional to the amount of candy?

Why or why not?

10.

Time (hours)	Snowfall (inches)
2	8
2.5	10
4	12
6	18

Is the snowfall proportional to the time?

Why or why not?

11.

Coffee (ounces)	6	8	14
Price (dollars)	2.10	2.80	4.90

Is the price proportional to the amount of coffee?

Why or why not?

In the following tables y is proportional to x . Fill in the table and state the constant of proportionality.

12.

x	y
2	8
5	20
	40
12	

$$k = \underline{\hspace{2cm}}$$

13.

x	y
8	4
6	3
	5
14	

$$k = \underline{\hspace{2cm}}$$

14.

x	20	4	8	
y	15		6	9

$$k = \underline{\hspace{2cm}}$$

Fill in the table and answer the questions.

15. The number of teachers at Generic Middle School is proportional to the number of students.

- How many students are there for one teacher?
- If there are 14 teachers at Generic Middle School, how many students are there?

Teachers	Students
2	
	80
4	64
9	

1. Determine if y is proportional to x . Explain why or why not.

x	4	12	28	36
y	1	4	7	9

Proportional? YES or NO

Explanation:

2. In the table y is proportional to x . Fill in the table and state the constant of proportionality.

x	y
4	12
2	
6	18
	24

$$k = \underline{\hspace{2cm}}$$

3. The amount of sugar in lemonade is proportional to the number of glasses.

- Find the constant of proportionality. What does it mean in this situation?
- Fill in the missing values on the table.
- If there are 177 grams of sugar, how many glasses are there?

Glasses (#)	Sugar (grams)
2	
	60
4	48
9	
5.5	

EXIT TICKET –

Neptune loves to swim. He swims 9 laps in 2 minutes.

Which table represents Neptune?

A

Time (minutes)	Laps (#)
0	0
9	2
18	4
27	6

B

Time (minutes)	Laps (#)
0	4.5
2	9
4	18
6	27

C

Time (minutes)	Laps (#)
0	0
2	9
4	18
6	27

D

Time (minutes)	Laps (#)
4.5	0
9	2
18	4
27	6